

A new interface between GAP and Singular: libsing

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Overview

- 1 What is this all about?
- 2 A very short example
- 3 The gory details

The protagonists

- “**GAP** is a system for computational discrete algebra, with particular emphasis on Computational Group Theory.
- “**Singular** is a computer algebra system for polynomial computations, with special emphasis on commutative and non-commutative algebra, algebraic geometry, and singularity theory. **Singular** provides highly efficient core algorithms, a multitude of advanced algorithms in the above fields, [...]”
- **libsing** provides an efficient bridge between these two systems.

Related work

- [GAP](#) package “singular” by Marco Costantini and Willem de Graaf
 - Last regular update in 2006, based on Singular 2
 - Uses “screen scraping” \rightsquigarrow fragile; inefficient
 - No generic way to transfer complex data structures.
 - No easy access to complete functionality of [Singular](#).
- Packages “IO_ForHomalg” & “RingsForHomalg by homalg project
 - Supports [Singular](#) 3 and 4
 - Based on IO package, but in the end also does “screen scraping”
 - Avoids data conversions where possible \rightsquigarrow efficient at what it does
 - Does not attempt to give access to complete functionality of [Singular](#) “out of the box”.
- [Sage](#) includes both [GAP](#) and [Singular](#), could be used as “interface”

Features

- `libsing` is a `GAP` package, loaded by the `GAP` interpreter, but also links against `Singular` 4 (compiled as a shared library).
- `libsing` consists of a part written in C++, and a part written in the `GAP` programming language.
- `libsing` grants access to the complete functionality of `Singular` from the high-level `GAP` programming language. With it you may ...
 - ... access `Singular` objects via `GAP` wrapper objects;
 - ... convert between `Singular` and `GAP` objects;
 - ... access `Singular` C++ kernel functions;
 - ... use `Singular` interpreter intrinsics;
 - ... use `Singular` libraries;all from within `GAP`.

Short example: Singular version

The following example is taken from the [Singular](#) manual, specifically from the entry for `stdfglm`, a library command for computing a Gröbner basis.

```
> ring r = 0, (x,y,z), lp;  
> ideal i = y3+x2, x2y+x2, x3-x2, z4-x2-y;  
> stdfglm(i);  
_[1]=z12  
_[2]=yz4-z8  
_[3]=y2+y-z8-z4  
_[4]=xy-xz4-y+z4  
_[5]=x2+y-z4
```

Short example: Straight conversion to GAP

The following is a straight conversion to [GAP](#) code using the low-level access to [Singular](#) interpreter intrinsics and library functions.

```
gap> r := SI_ring(0, ["x", "y", "z"], [{"lp", 3}]);  
<singular ring>  
gap> i := SI_ideal(r, "y3+x2,x2y+x2,x3-x2,z4-x2-y");  
<singular ideal (mutable), 4 gens of deg <= 4>  
gap> SIL_stdfglm(i);  
<singular ideal (mutable), 5 gens of deg <= 12>  
gap> Display(last);  
z12,  
yz4-z8,  
y2+y-z8-z4,  
xy-xz4-y+z4,  
x2+y-z4
```

Short example: Better GAP version

Or we can do without those strings and use a more “GAP-style” way of entering the polynomials:

```
gap> r := SI_ring(0, ["x", "y", "z"], [{"lp", 3}]);;
gap> AssignGeneratorVariables(r);
#I Assigned the global variables [ x, y, z ]
gap> i := SI_ideal([y^3 + x^2, x^2*y + x^2,
>                 x^3 - x^2, z^4 - x^2 - y]);
<singular ideal (mutable), 4 gens of deg <= 4>
gap> SIL_stdfglm(i);
gap> Display(last);
z12,
yz4-z8,
y2+y-z8-z4,
xy-xz4-y+z4,
x2+y-z4
```

Troubled data exchange

- **GAP** and **Singular** deal with many similar kinds of data: machine integers, multiprecision integers, lists, matrices, polynomials, etc.
- ... but they represent them quite differently.
- They also use radically different memory management schemes:
- **GAP**: generational moving garbage collector
 - memory does not have to be explicitly released;
 - the exact location of an object in memory can change.
- **Singular**: traditional memory manager plus reference counting
 - memory must be freed explicitly;
 - objects live in a fixed position during their life time.
- Need to bridge these differences with as little overhead as possible.

Wrapping objects

- **Singular** objects to be used from **GAP** are put into wrapper objects.
- **Singular** objects stay in a fixed place, the **GAP** wrapper may move.
- Benefit from the garbage collector housekeeping: if the wrapper is garbage collected, we free the wrapped object.
- **Singular** has a notion of an “active ring”, implicitly used for computations. **libsing** hides this concept from **GAP** and the user.

Wrapping objects II

There are three kinds of wrappers, consisting of two or four machine words (32 or 64 bit), respectively. Namely for ...

ring free objects:

Attribute bits & type
C++ pointer to Singular object

ring dependant objects:

Attribute bits & type
C++ pointer to Singular object
GAP reference to wrapper for ring
C++ pointer to Singular ring

rings:

Attribute bits & type
C++ pointer to Singular object
GAP reference to wrapper for ring's zero
GAP reference to wrapper for ring's one

There can also be an additional word for the extended attributes.

Converting data

- (Un)wrapping objects is fast, has low memory overhead.
- But sometimes one needs to convert data, e.g.: given some **GAP** data, convert it to **Singular**, perform heavy computations, convert the result back to **GAP**.
- Machine ints are converted directly.

```
gap> SI_int(3);  
3
```

- Multi precisions ints: **GAP** uses low-level, **Singular** high-level GMP interface \implies conversion is necessary, requires copying data.

```
gap> x := SI_bigint(3^20);  
<singular bigint:3486784401>  
gap> _SI_Intbigint(x);  
3486784401
```

Converting data II

- Containers (intvecs, intmats, lists, etc.) are converted recursively.

```
gap> v := SI_intvec([1,2,3]);  
<singular intvec:[ 1, 2, 3 ]>  
gap> _SI_Plistintvec(v);  
[ 1, 2, 3 ]
```

- Rings, their elements, ideals, ..., are not (automatically) converted, (exception: rationals, $\mathbb{Z}/p\mathbb{Z}$)

```
gap> r := SI_ring(0, ["x", "y", "z"], [{"lp", 3}]);  
<singular ring>
```

- Instead of converting e.g. polynomials, the goal is to implement high level [GAP](#) APIs for such objects (e.g. querying the degree, coefficients, etc.).

Low level: Calling into the Singular kernel

- Wrappers for select C / C++ functions from the [Singular](#) kernel.
- For each supported function, we copy its declaration from the [Singular](#) kernel, augmenting it with some “hints”:

```
poly pp_Mult_nn(poly p, number n, const ring r);  
poly p_Mult_nn(DESTROYS poly p, number n, const ring r);
```

- When compiling [libsing](#) (via `make`), this is read by a code generator, which produces C wrappers accessible from [GAP](#):

```
_SI_pp_Mult_nn  
_SI_p_Mult_nn
```

- Right now only a small set of functions is mapped, but it is very easy to extend this.

Middle level: Using interpreter intrinsics

- “Interpreter intrinsics”: functions provided by the [Singular](#) interpreter, but implemented in C++ (such as `betti`, `std`, `ncols`).
- Take different data types as input as the kernel functions.
- [Singular](#) interpreter contains a table describing all intrinsics (including names, parameter types; overloading possible)
- When compiling [libsing](#), this table is read and appropriate wrappers are created as [GAP](#) functions

```
BindGlobal("SI_degree",  
  function(a)  
    return _SI_CallFunc1(285,a);  
  end );
```

Middle level: Using Singular libraries

- Functions and libraries written in the [Singular](#) language are usable.

```
gap> SIL_submat;  
Error, Variable: 'SIL_submat' must have a value  
not in any function at line 44 of *stdin*  
gap> SI_LIB("matrix.lib");  
gap> s := SI_ring(0,["a","b"]);;  
gap> m := SI_matrix(s,2,2,"a,b,ab,1");  
<singular matrix (mutable):  
a, b,  
ab,1 >  
gap> y := SIL_submat(m,SI_intvec([1,2]),SI_intvec([2]));  
<singular matrix (mutable):  
b,  
1 >
```

- Currently can not use [GAP](#) functions from [Singular](#).

High level: Dressing it up as GAP objects

- Finally, we also intend to provide high-level GAP wrappers for Singular functionality.

- For example, operators like +, -, * are overloaded.

```
gap> SI_bigint(3^25) + SI_bigint(7^36);  
<singular bigint:2651730845859653472626311991044>
```

- This is still a lot of work if one wants to cover everything.